

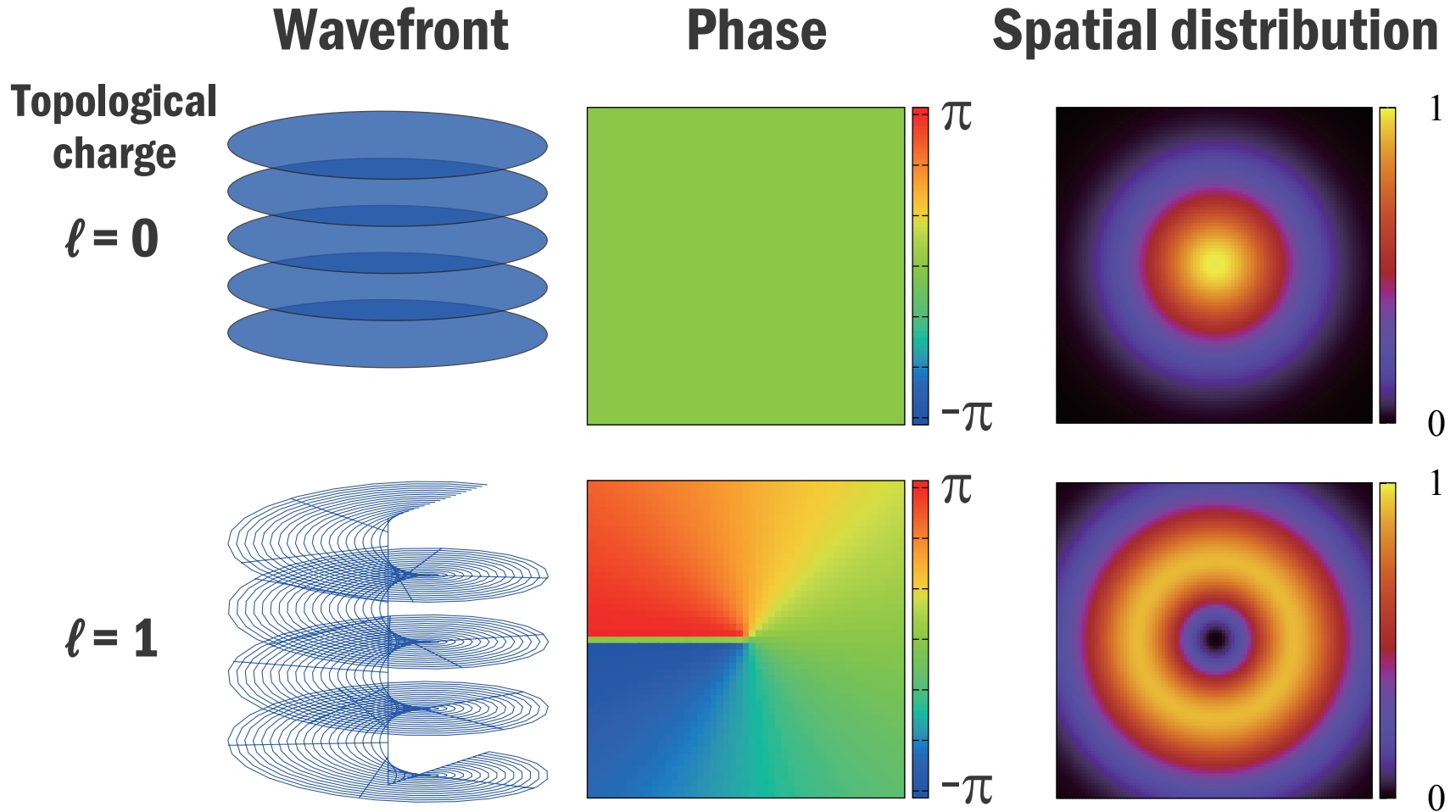
非線形逆トムソン散乱による ガンマ線渦の発生

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Optical vortices forming helical wavefronts



$$E \propto \exp(i\ell\phi)$$

Carrying $\ell\hbar$ orbital angular momentum (OAM)

Representative optical vortex: Laguerre Gaussian mode

Poynting vector and total AM

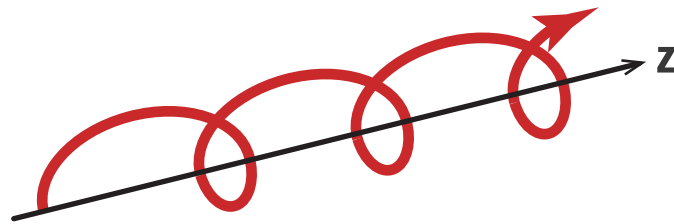
Poynting vector of Laguerre Gaussian mode

$$\mathbf{S} = \mathbf{E} \times \mathbf{B} \propto \left(\frac{\rho z}{z^2 + z_R^2} \mathbf{e}_\rho + \frac{\ell}{k\rho} \mathbf{e}_\phi + \mathbf{e}_z \right)$$

k: wave number of LG light
 ρ : distance from the z-axis

spread of the beam

Spiral Poynting vector gives OAM



Total angular momentum

$$\text{Spin AM} + \text{OAM} = \pm \hbar + \ell \hbar \text{ or } \ell \hbar$$

Circularly polarized
optical vortex

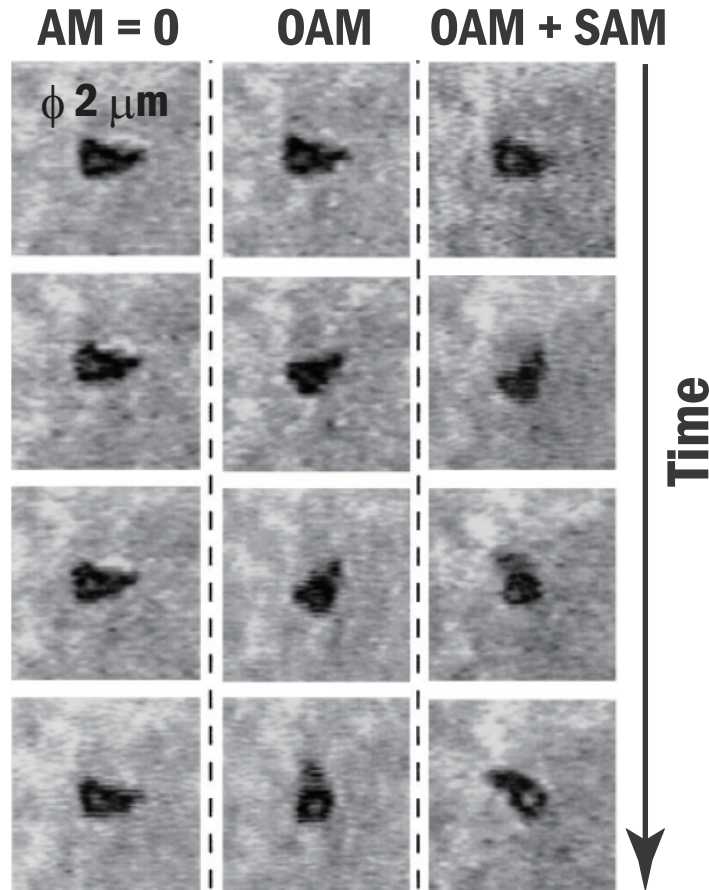
Linearly polarized
optical vortex

L. Allen et al., Phys. Rev. A 45 (1992) 8185.

L. Allen et al., Prog. Opt. 39 (1999) 291.

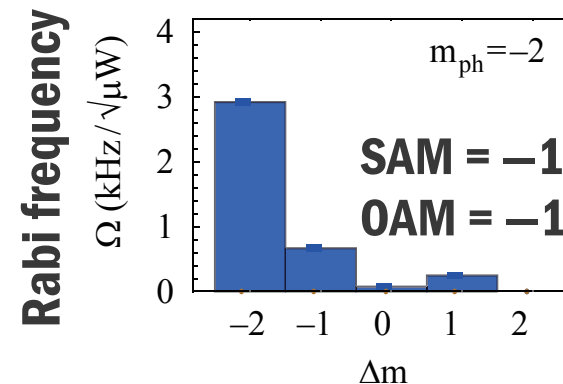
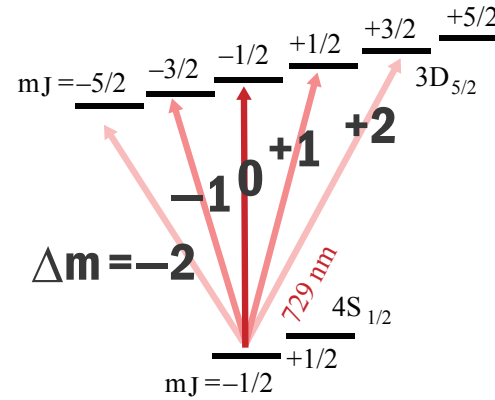
Transfer of OAM using optical vortex lasers

To a micro particle



To a valence electron

Quadruple transition at 729 nm of $^{40}\text{Ca}^+$ ion.



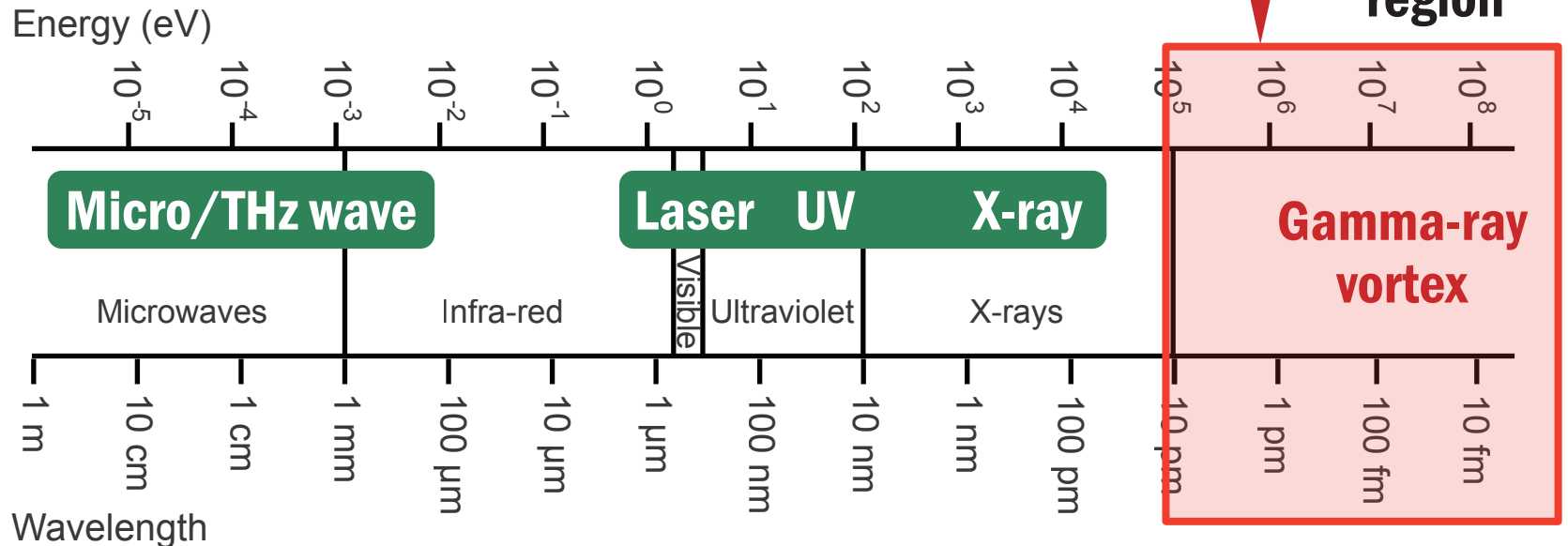
N. B. Simpson et al., Opt. Lett. 22 (1997) 52.

C. T. Schmiegelow et al., Nat. Comm. 7 (2016) 12998.

Purpose

Generation of gamma-ray vortices (more than sub-MeV energy) and development of their application.

Developed vortex beams



Except for the electromagnetic wave

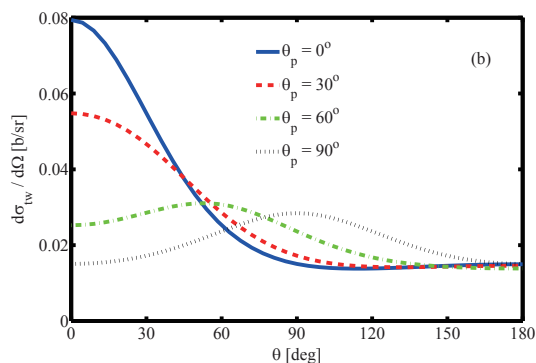
300 kV electron

Cold neutron

Applications of gamma-ray vortices

Compton scattering

J. A. Sherwin, Phys. Rev. A 96 062120 (2017).

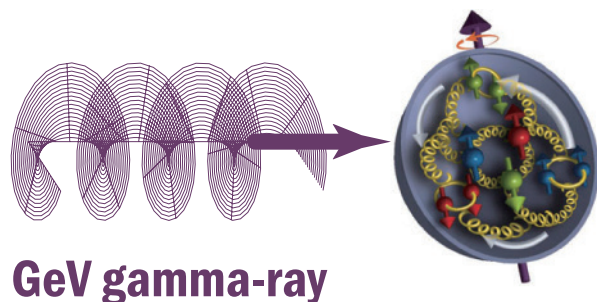


Cross section ($E_0 = 500$ keV)

θ_p : Momentum ratio between transverse and longitudinal component

They may be applied to solid state physics by being expanded to magnetic Compton scattering.

Insight into the proton structure



Proton spin puzzle: Only 30% of the proton spin is carried by the quark spin.

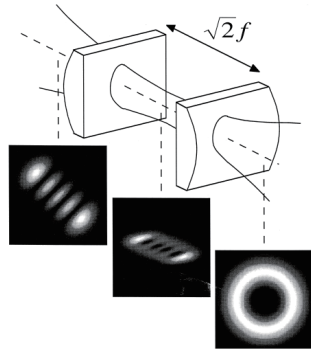
If OAM of gamma-rays affects to OAM of quark or gluon, it becomes novel probe of the proton spin.

Other potential application

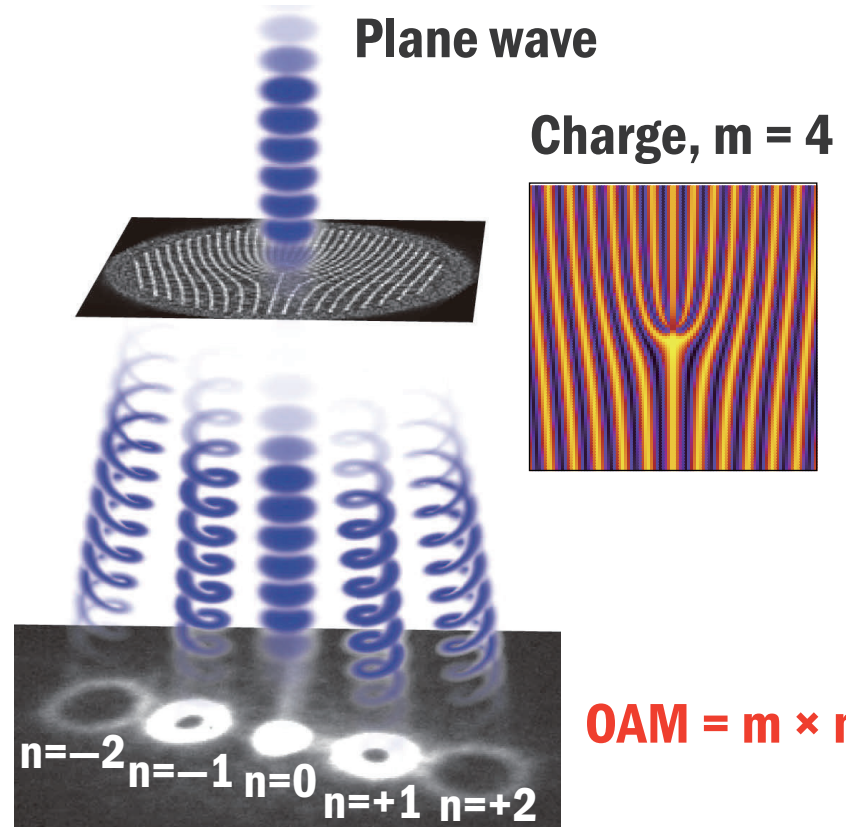
Excitation of nucleus, Generation of positron vortices, Astrophysics, etc.

Generation of optical vortices

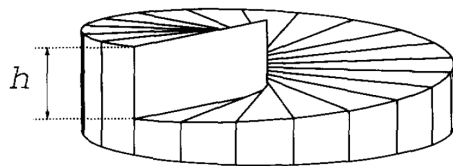
Cylindrical lens



Fork grating



Spiral phase plate

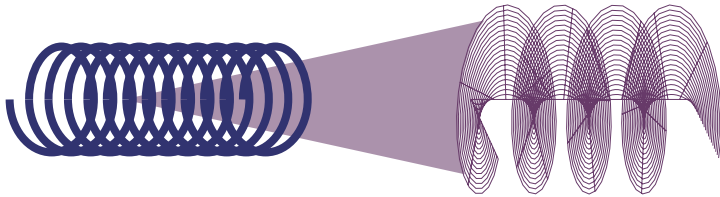


- J. Courtial et al., Opt. Comm. 159 (1999) 13.
M. W. Beijersbergen et al., Opt. Comm. 112 (1994) 321.
B. J. McMorran et al., Science 331 (2011) 192.

Optical vortices from free electrons

An electron moving on a circular trajectory emits optical vortices

Electron



Electric field emitted by a helical undulator

$$\mathbf{E} \propto C \exp \{ i(n-1)\phi \} \mathbf{e}_+$$

n^{th} higher harmonics carry $(n-1)\hbar$ OAM

S. Sasaki et al., PRL. 100 124801 (2008).

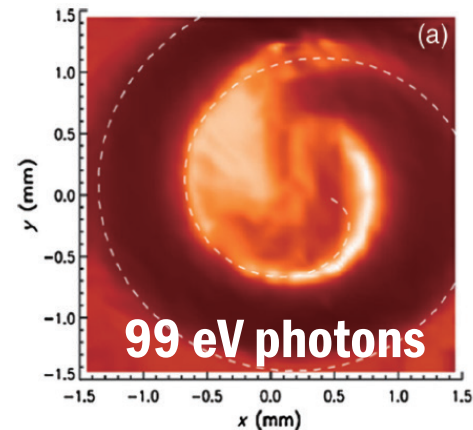
M. Katoh et al., PRL. 118 094801 (2017).

This was demonstrated in ultraviolet and soft X-ray regions.

2nd harmonics (1 \hbar OAM)  1 spiral interference fringe (Helical + Spherical)

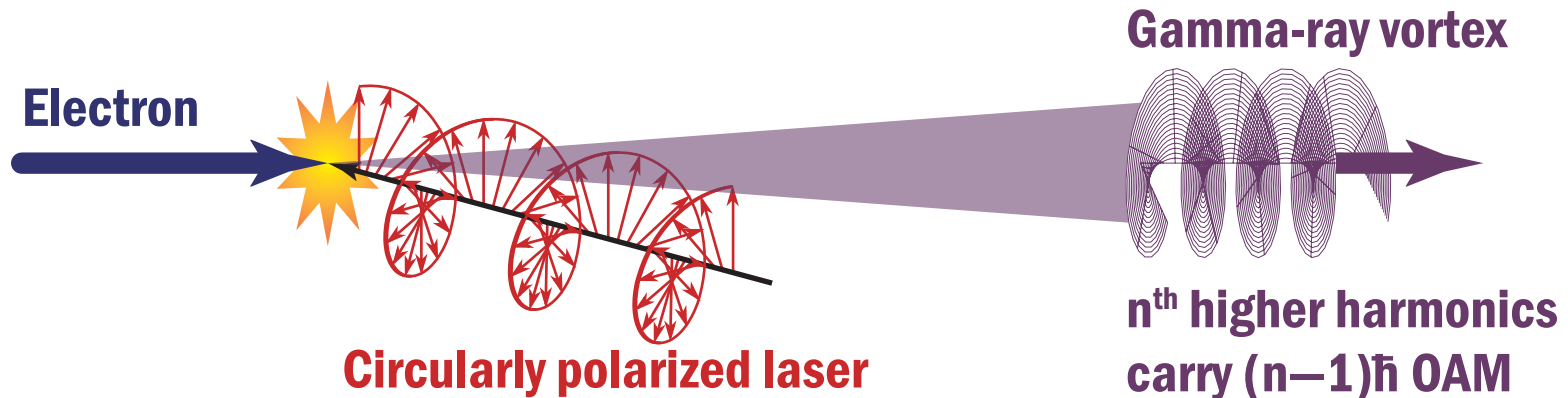
J. Bahrtdt et al., PRL 111 034801 (2013).

M. Katoh et al., Sci. Rep. 7 6130 (2017).

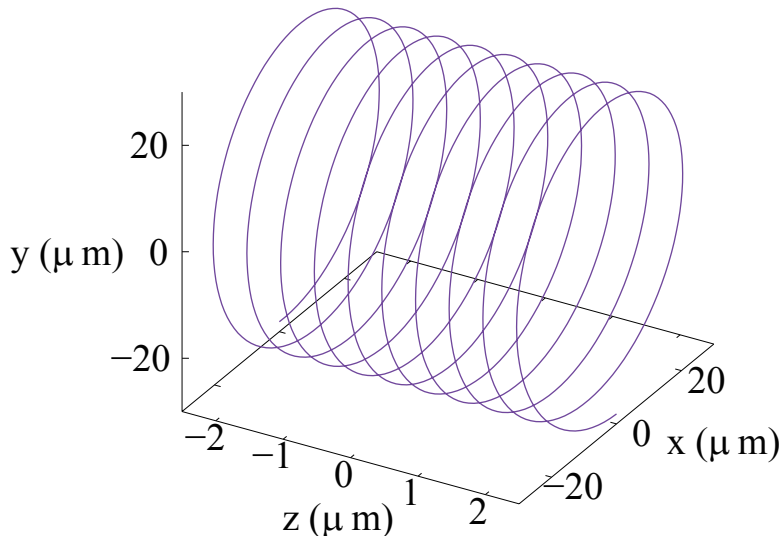


Gamma-ray vortices via NITS

Nonlinear inverse Thomson scattering (NITS)



Electron trajectory inside a laser



Gamma-ray energy

$$E_{\gamma} = \frac{4n\gamma_0^2 E_L}{1 + a_0^2/2}$$

γ_0 : Lorentz factor of an electron

E_L : Energy of laser photon

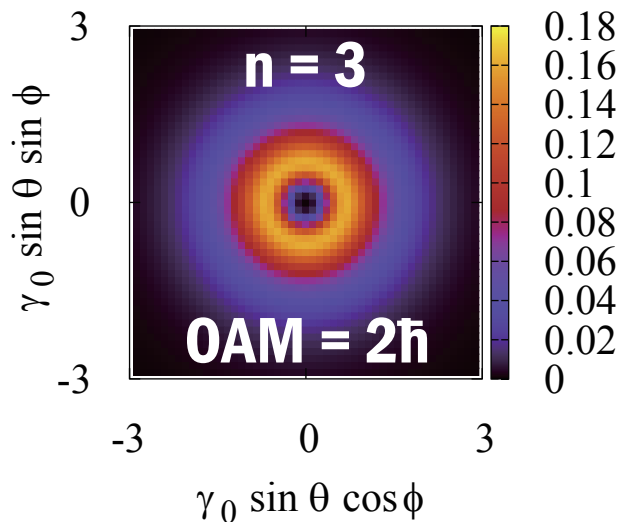
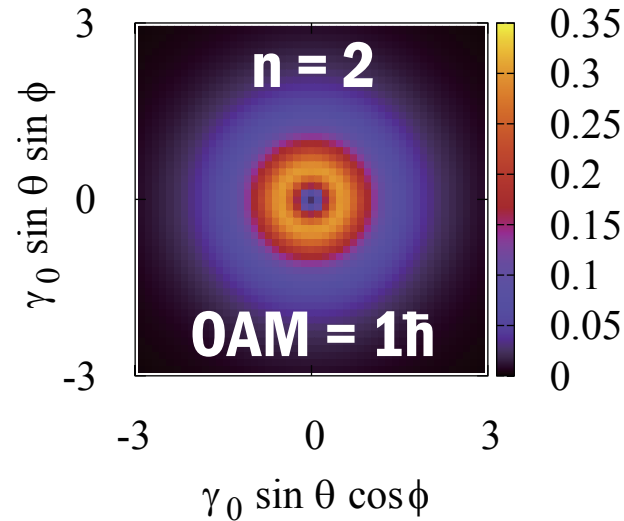
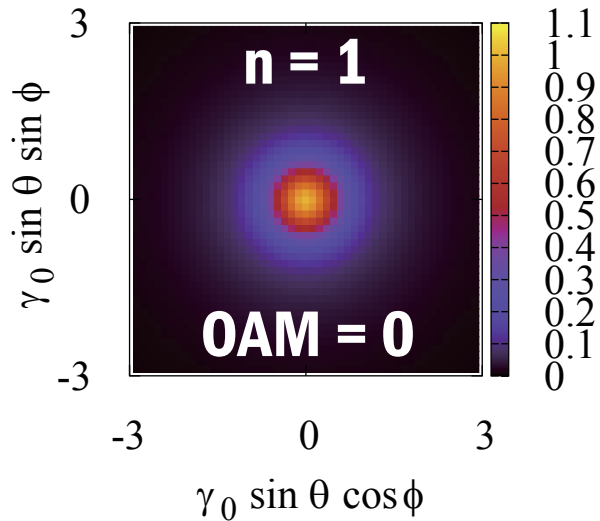
a_0 : Laser strength parameter

10^{18} W/cm^2 reaches $a_0 \approx 1$

Y. Taira et al., Sci. Rep. 7 5018 (2017).

Y. Taira et al., The Astrophysical Journal 860 45 (2018).

Spatial distributions of NITS gamma-rays

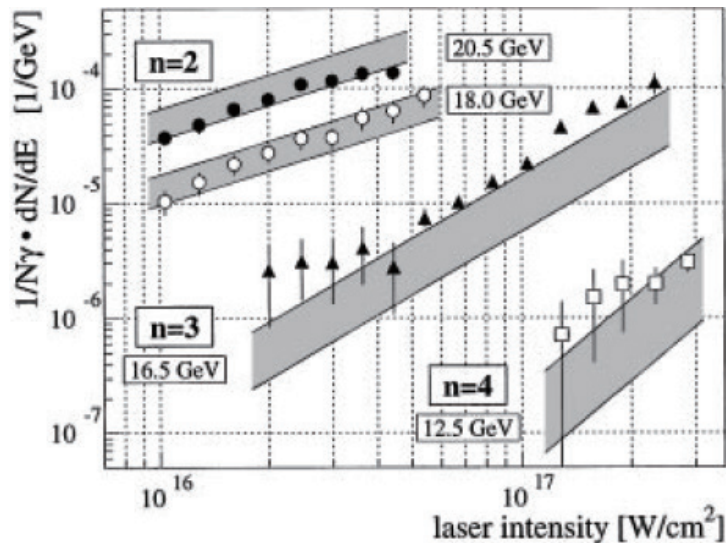
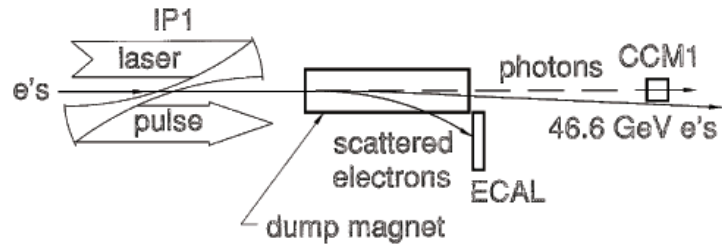


Only higher harmonic gamma-rays show annular intensity distribution, which is consistent with the characteristics of an optical vortex.

NITS using RF accelerated electrons

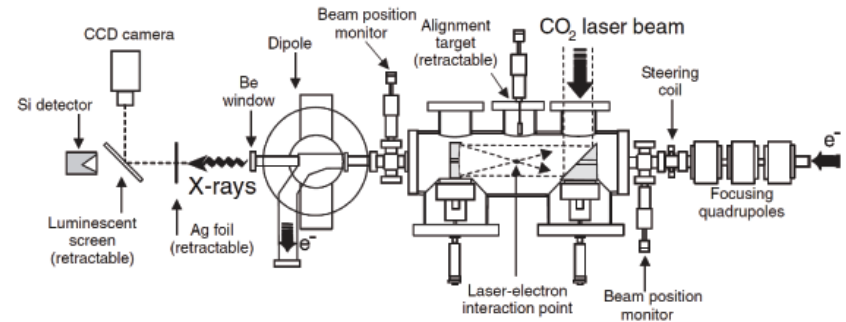
SLAC

C. Bula et al., PRL 76 3116 (1996).

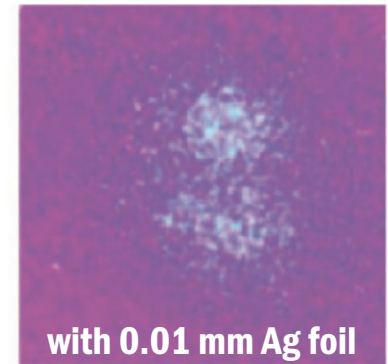
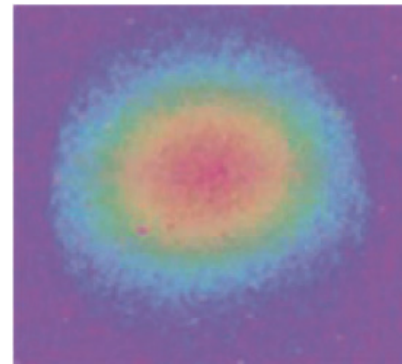


BNL

M. Babzien et al., PRL 96 054802 (2006).



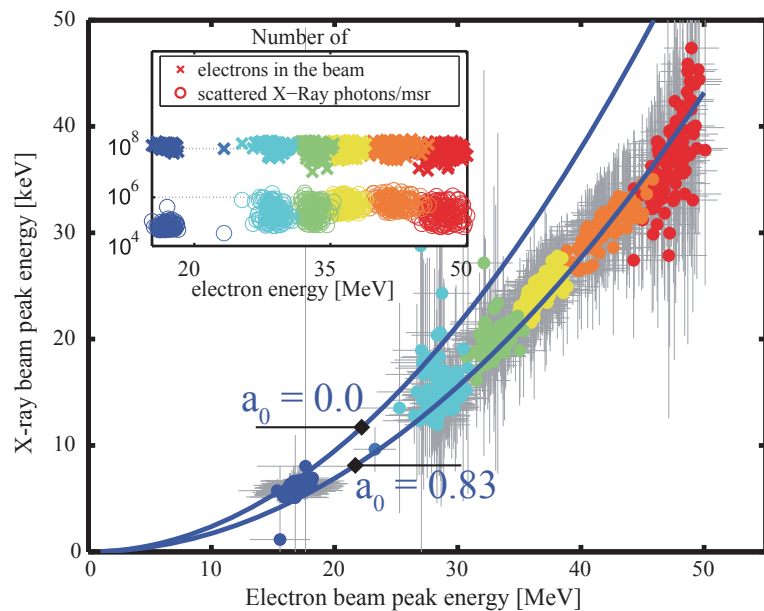
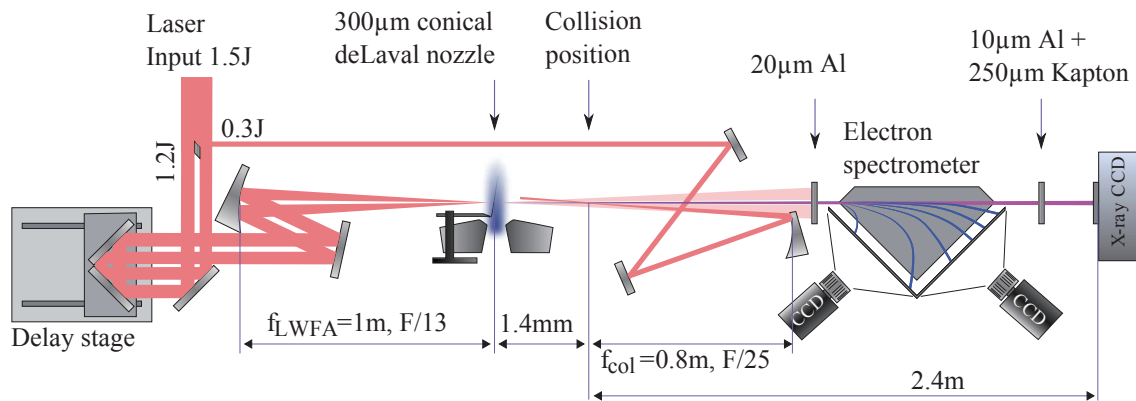
Spatial distributions of linearly polarized X-rays



NITS using laser wakefield accelerated e-

Ludwig-Maximilians-Universität München

K. Khrennikov et al., PRL 114 195003 (2015).



AIST

E. Miura et al., APEX 7 046701 (2014).

U of Nebraska-Lincoln

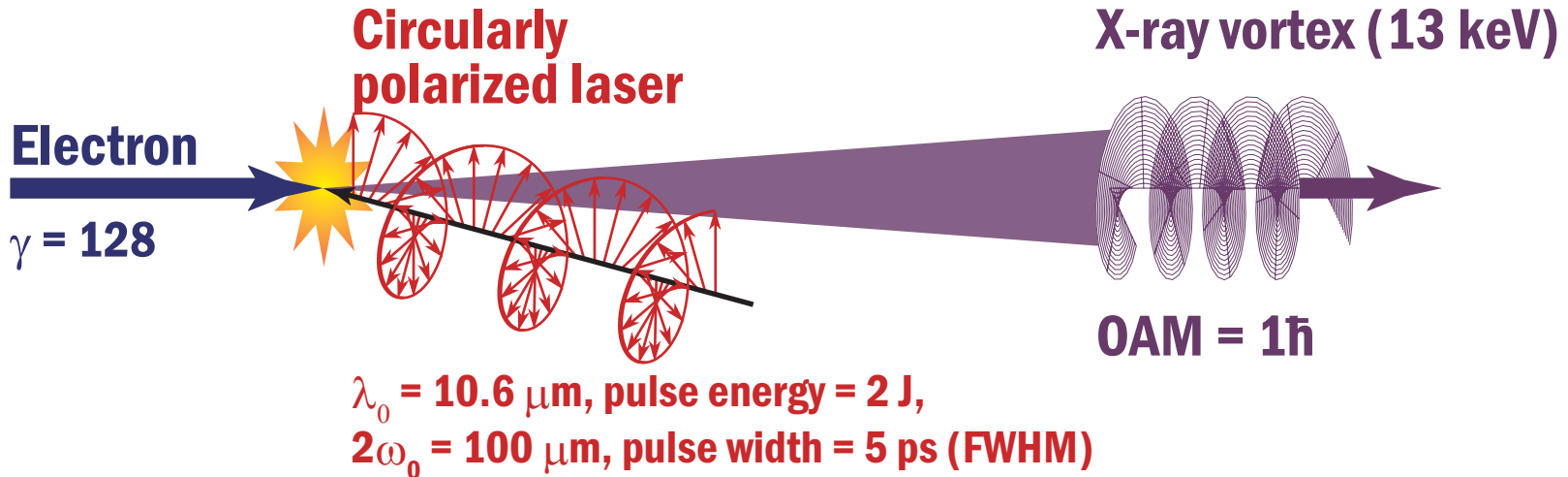
W. Yan et al., Nat. Phot. 11 514 (2017).

Rutherford Appleton Laboratory

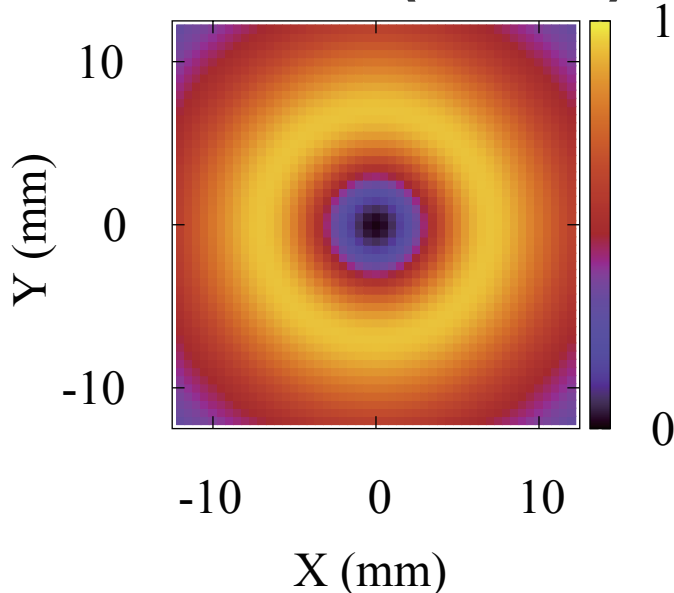
G. Sarri et al., PRL 113 224801 (2014).

J. M. Cole et al., PRX 8 011020 (2018).

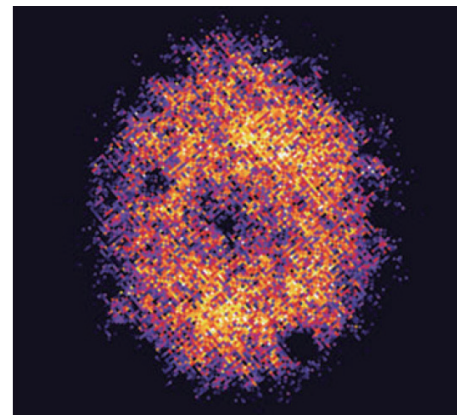
Second harmonic X-rays at BNL ($a_0=0.6$)



Calculation (Y. Taira)



Measurement (BNL)



E = 13 keV ($\lambda = 0.095 \text{ nm}$)

This will be a X-ray vortex.

Next step

Measurement of a helical wavefront.

Experimental plans at KPSI and UVSOR-III

KPSI of QST

Microtron + J-KAREN-P PW laser (800 nm)



$$\gamma_0 = 300$$
$$a_0 < 3$$



0.4 MeV gamma-ray vortices.

$$N_\gamma = 10^3 \sim 10^5 \text{ photons/sec}$$

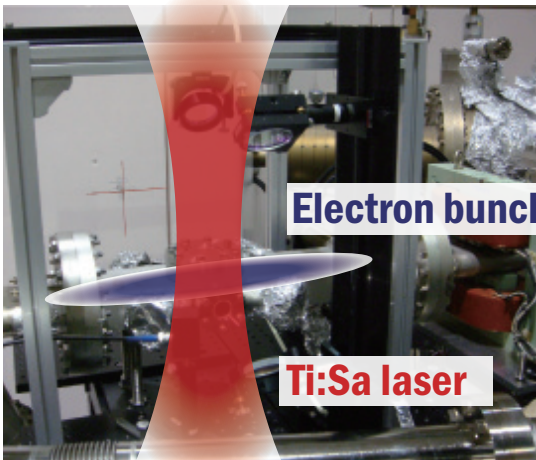
Purpose:

Measurement of annular distribution and helical wavefront.

Study of Compton scattering.

UVSOR-III

90-degree collision



$$\gamma_0 = 1470$$
$$a_0 \sim 0.6$$



10 MeV gamma-ray vortices.

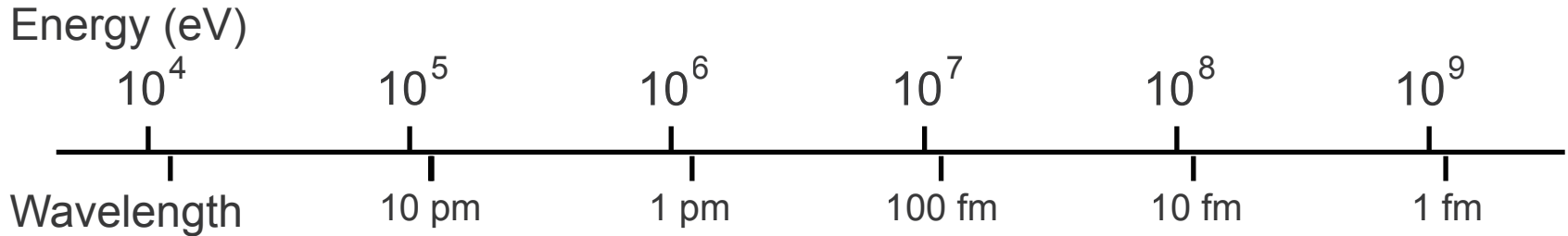
$$N_\gamma \sim 800 \text{ photons/sec}$$

Purpose:

Measurement of annular distribution.

Study of Compton scattering and nuclear excitation.

Measurement of γ -ray vortex is challenging



~10 keV

Interference

Diffraction

1 MeV ~ 30 MeV

Nuclear excitation

Compton scattering

0.1~10 MeV

1 MeV <

Pair production

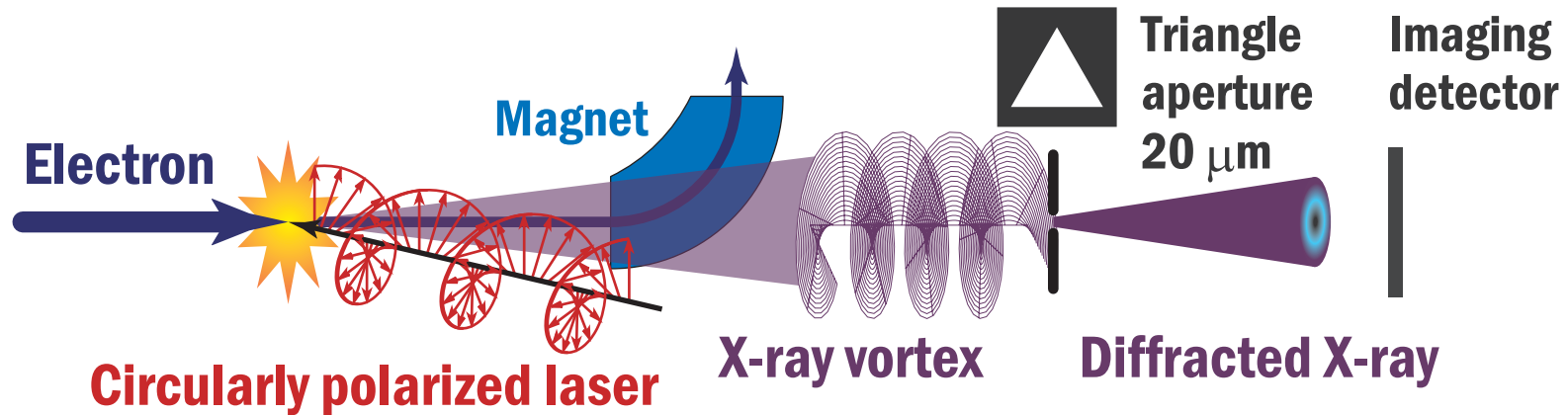
1 GeV <

Interaction with hadrons

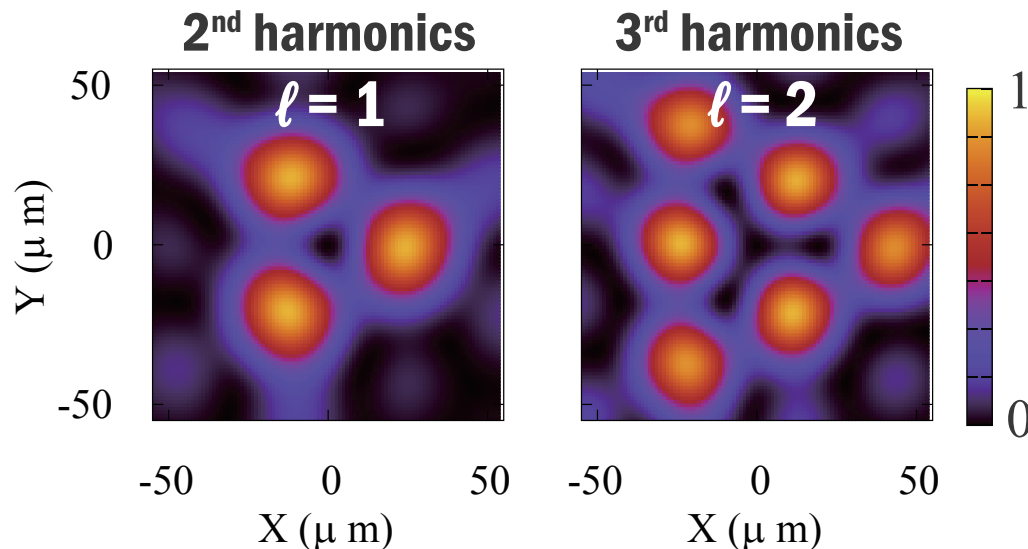
Explore measurement methods of γ -ray vortices

Diffraction method

Triangle aperture



Calculated diffraction pattern (5keV)



A triangle aperture can be used to measure the helical wavefronts.

R&D is carried out at SPring-8.

Acknowledgment

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Summary

- **Gamma-ray vortices can be generated by nonlinear inverse Thomson scattering.**

n -th higher harmonic gamma-rays carry $(n-1)\hbar$ OAM.

- **Measurement of gamma-ray vortices is a big issue.**

In the low energy region, diffraction and interference methods must work.

Compton scattering may work around MeV energy region.

Thank you for your attention!